

92. Parallax: $D (pc) = \frac{1}{p (arcsec)} = \frac{1}{0.002} = 500 pc$

93. Distance modulus: $d (pc) = 10^{m-M+5/5} = 10^{(5.4+19.6+5)/5} = 10^{30/5} = 1,000,000 pc$

94. Distance modulus is defined as $m - M$. The absolute magnitude M is defined to be the apparent magnitude at a distance of 10 pc, so $m - M$ would equal zero at 10 pc.

Alternately: $d (pc) = 10^{(0+5)/5} = 10^1 = 10 pc$

95. By definition, 5 magnitudes is equal to a factor of 100 in brightness. So this object is now 1/100 times as bright.

Alternately, use the distance modulus: Say the object originally has $M = 0$, $m = 0$.

$$d_0 = 10^{(0-0+5)/5} = 10^1 = 10 pc$$

$$d_{dim} = 10^{(5-0+5)/5} = 10^2 = 100 pc$$

By the inverse square law, brightness (or flux) is proportional to $\frac{1}{d^2}$, so if the same object is 10 times further, it is 1/100 times as bright.

96. This question is based on the LRT relation, $L = R^2 T^4$.

a. $L_{new} = (5R)^2 T^4 = 25 L$

b. $L_{new} = R^2 (3T)^4 = 81 L$

c. $L_{new} = (8R)^2 \left(\frac{1}{2}T\right)^4 = 64 R^2 * \frac{1}{16} T^4 = 4 L$

97. This question is based on the inverse square law, $\propto \frac{1}{d^2}$, which can also be written $\frac{F}{F_0} = \frac{d_0^2}{d^2}$.

a. $F = \frac{(1 AU)^2}{(0.4 AU)^2} F_0 = \frac{1}{(2/5)^2} \left(1 \frac{W}{m^2}\right) = \frac{25}{4} \left(1 \frac{W}{m^2}\right) = 6.25 \frac{W}{m^2}$

b. $F = \frac{(1 AU)^2}{(5 AU)^2} F_0 = \frac{1}{25} \left(1 \frac{W}{m^2}\right) = 0.04 \frac{W}{m^2}$

98. This question and the next one are based on Wien's Law, $\lambda_{max} = \frac{b}{T}$. The constant b is usually equal to $2.898 * 10^6 nm K$, but setting it equal to $3 * 10^6 nm K$ makes things easier.

a. $\lambda_{max} = \frac{(3*10^6 nm K)}{30,000 K} = 100 nm$

b. Ultraviolet (violet is ~300 nm)

99.

a. $\lambda_{max} = \frac{(3*10^6 nm K)}{3,000 K} = 1000 nm$

b. Infrared (red is ~700 nm)

100.

a. Use the Stefan-Boltzmann Law, $F = \sigma T^4$

$$F = \left(6 * 10^{-8} \frac{W}{m^2 K^4}\right) (10,000 K)^4 = \left(6 * 10^{-8} \frac{W}{m^2 K^4}\right) 10^{16} K^4 = 6 * 10^8 \frac{W}{m^2}$$

b. Luminosity is just flux times area, in this case surface area.

$$L = F * A = \left(6 * 10^8 \frac{W}{m^2}\right) (1 * 10^{19} m^2) = 6 * 10^{27} W$$